

# Chapter 15: Government and Public Policies

## Graduate Macroeconomics Slides

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# Outline

- Introduction and Motivation
- Public Finance: An Overview of the Data
- Distortionary Taxes and Neoclassical Growth
- Government Debt and Ricardian Equivalence
- Ramsey Taxation
- Overlapping Generations: Debt and Pensions
- Redistribution: Taxes and Transfers
- Conclusion and References



# Chapter Overview

- The government has large impact on the economy via *fiscal*, *monetary*, and *regulatory* policies.
- This chapter focuses on **fiscal policy**: taxes, government spending, and debt.
- Main themes:
  - How governments tax, spend, and borrow in practice.
  - How fiscal policy choices shape competitive equilibrium allocations.
  - The trade-offs in optimizing over policy choices (*Ramsey* approaches, redistribution, *time consistency*, etc.).



# Why Governments Intervene

## Three main rationales for government intervention:

### 1. Public Goods and Externalities:

- Public goods (e.g., national defense) cannot be well-excluded to non-payers.
- Large positive externalities in education, healthcare, vaccinations, etc.

### 2. Incomplete Markets and Information Frictions:

- Private insurance might be missing (e.g., unemployment insurance, annuities).
- Government can provide social insurance or bailouts during crises (e.g., 2008 Global Financial Crisis).

### 3. Redistribution:

- Markets can yield significant inequality.
- Government taxes the rich to fund transfers to the poor.



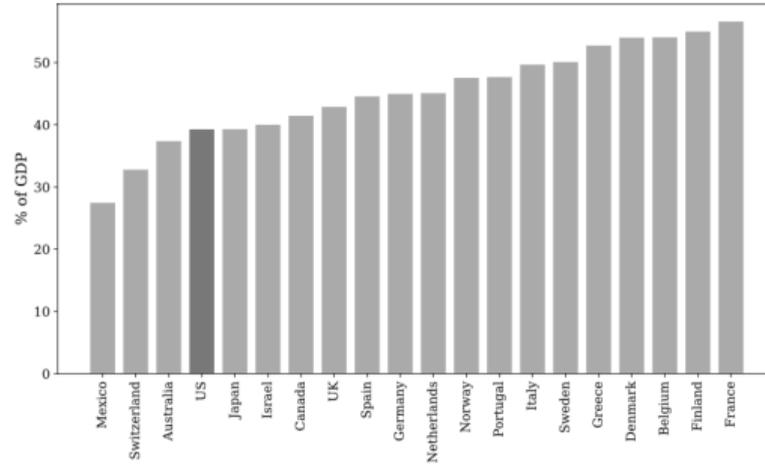


Figure 15.1: Government Spending across Countries (avg. 2010-2019).



# Public Finance: An Overview of the Data

1. What the government does: spend, transfer, tax, borrow.
2. Budget identity and the definition of deficits/debt.
3. U.S. facts: revenues vs outlays; tax mix; deficits; debt.
4. Debt-to-GDP dynamics and a simple sustainability rule.
5. Composition of spending over time; automatic stabilizers.



# Government budget identity

$$\underbrace{G_t + T_t}_{\text{primary outlays}} + \underbrace{i_t B_{t-1}}_{\text{interest}} = \underbrace{Rev_t}_{\text{taxes}} + \underbrace{B_t - B_{t-1}}_{\text{net borrowing}} \quad (\text{Eq. 15.1})$$

- **Primary deficit:**  $D_t \equiv G_t + T_t - Rev_t$  (excludes interest).
- **Debt accumulation:**  $B_t = (1 + i_t)B_{t-1} + D_t$ .
- Read left-to-right: if outlays  $>$  revenues, the gap is financed by new borrowing.



# Revenues vs expenditures

- Both trend up to 1970, then roughly stabilize as % of GDP.
- Expenditures typically exceed revenues  $\Rightarrow$  deficits on average.
- Large spikes in spending during wars and recessions.

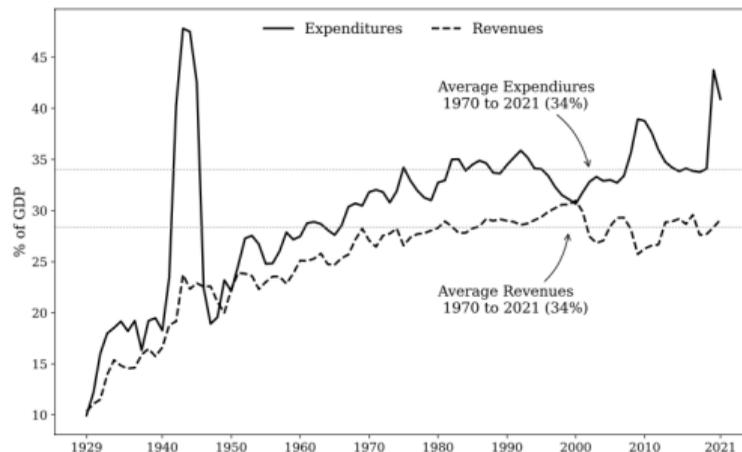


Figure 15.2: Revenues and Outlays, as percentages of GDP.



# Where tax dollars come from

- Over the postwar era: income taxes and social insurance contributions rose.
- Sales/import taxes roughly flat; corporate tax share declined.
- Policy takeaway: different tax bases move differently with the cycle.



Figure 15.3: Taxes by Category, as percentages of GDP.



# Deficits and debt over time

## Left panel (deficits):

- Total deficit = primary deficit + net interest.
- Wars/recessions: deficits widen sharply.
- Evidence of *tax smoothing*: borrowing rises in bad times.

## Right panel (debt stock):

- Debt-to-GDP rises in major crises; falls in booms/inflationary eras.
- State vs federal composition varies by country; U.S. mostly federal.



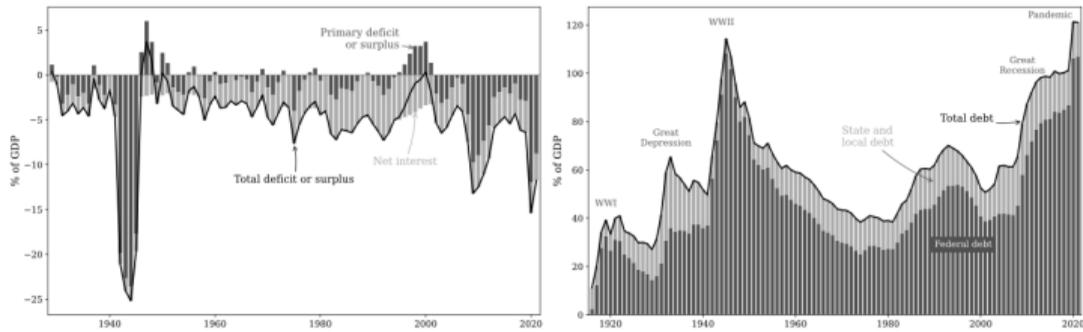


Figure 15.4: Left: Total Deficits, Primary Deficits, and Net Interest Outlays. Right: Total Debt. All as percentages of GDP.

# From nominal debt to debt/GDP dynamics

Start with *levels*:

$$B_t = (1 + i_t)B_{t-1} + D_t.$$

Divide by nominal GDP,  $P_t Y_t$ ; define  $b_t \equiv B_t/(P_t Y_t)$ ,  $d_t \equiv D_t/(P_t Y_t)$ ,  $\pi_t \equiv P_t/P_{t-1} - 1$ ,  $\gamma_t \equiv Y_t/Y_{t-1} - 1$ :

$$b_t = \frac{1 + i_t}{(1 + \pi_t)(1 + \gamma_t)} b_{t-1} + d_t$$

Using the ex post real interest factor  $1 + r_t = \frac{1+i_t}{1+\pi_t}$ :

$$b_t = \frac{1 + r_t}{1 + \gamma_t} b_{t-1} + d_t$$

*Plain English:* debt/GDP rises when interest beats growth and/or when the primary deficit is large.



# Simple sustainability rule-of-thumb

Hold  $r, \gamma$  and target a constant ratio  $b_t = b_{t-1} = \bar{b}$ . Solve

$$\bar{b} = \frac{1+r}{1+\gamma} \bar{b} + \bar{d} \quad \Rightarrow \quad \boxed{\bar{d} = \frac{\gamma - r}{1 + \gamma} \bar{b}} \quad (\text{Eq. 15.2})$$

**Numerical example:**

$$r = 0.02, \quad \gamma = 0.03, \quad \bar{b} = 1.00 \Rightarrow \bar{d} = \frac{0.03 - 0.02}{1.03} \times 1 \approx 0.0097 \quad (\approx 1\% \text{ of GDP}).$$

*Cautions:* if  $b$  rises,  $r$  may rise (risk premia/market depth); if  $r > \gamma$  later, stabilizing requires primary surpluses.



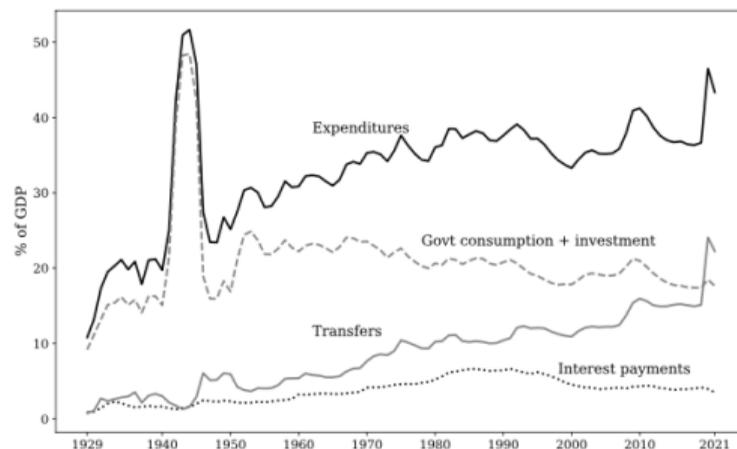
# How much debt is “too much”?

- When  $r < \gamma$ , constant *fractional* primary deficits can stabilize even high  $\bar{b}$  (arithmetic), but market responses can flip  $r - \gamma$ .
- Sustainability depends on future  $r, \gamma$  paths, tax capacity, political economy, and rollover risk.
- Use rule-of-thumb for *ballpark*, not a guarantee.



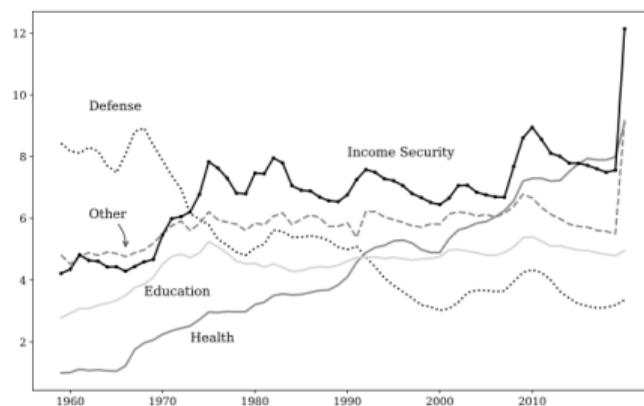
# Where the money goes by economic category

Early postwar: government consumption & investment dominated; later: transfers surged (e.g., Social Security, UI), interest varies with  $r$  and  $b$ .



# Where the money goes by function

- Education roughly stable around 5% of GDP.
- Defense peaked near 1959 then declined to  $\sim 3\%$ .
- Health (Medicare/Medicaid) rose steadily to  $> 8\%$ .
- **Income security** (UI, retirement, disability, welfare)  $\sim 7\%$  and *countercyclical*  $\Rightarrow$  “automatic stabilizers.”



# Summary of Public Debt and Public Finance

- Budget identity is an accounting truth; dynamics of  $b_t$  hinge on  $(r - \gamma)$  and the primary balance.
- U.S. runs deficits on average; debt rises in wars/recessions; transfers and health have grown over time.
- Rule-of-thumb: with  $r \approx 2\%$ ,  $\gamma \approx 3\%$ , and  $b \approx 100\%$ , a  $\sim 1\%$  primary deficit stabilizes  $b$  — *subject to market feedbacks*.
- Automatic stabilizers (UI, safety net) drive countercyclical outlays without new legislation.



# First Welfare Theorem and Market Failures

- Recall from Chapter 6: **First Welfare Theorem** requires complete markets, no externalities, no public goods.
- If these conditions fail, *competitive equilibria* may *not* be Pareto efficient.
- Government interventions then can improve welfare via:
  - Provision of public goods / correction of externalities.
  - Insurance where private markets fail.
  - Redistribution for equity considerations.



# A Neoclassical Framework with Taxes

## Setup:

- Households: infinitely-lived, discount factor  $\beta$ , utility  $u(c_t, l_t)$ .
- Production:  $y_t = f(k_t, l_t)$ , with competitive factor prices  $w_t, r_t$ .
- Govt. finances  $G_t$  and  $T_t$  (transfers) via taxes:

$\tau_{c,t}$  (consumption),  $\tau_{l,t}$  (labor income),  $\tau_{k,t}$  (capital income).

- No government debt here (introduced later). The budget:

$$G_t + T_t = \tau_{c,t} C_t + \tau_{l,t} w_t L_t + \tau_{k,t} (r_t - \delta) K_t.$$

- Household budget constraint:

$$(1 + \tau_{c,t}) c_t + k_{t+1} = (1 - \tau_{l,t}) w_t l_t + (1 - \tau_{k,t})(r_t - \delta) k_t + T_t.$$



# Distortionary Effects

**Household's FOC for saving:**

$$\frac{1 + \tau_{c,t+1}}{1 + \tau_{c,t}} u_c(c_t, l_t) = \beta [1 + (1 - \tau_{k,t+1})(r_{t+1} - \delta)] u_c(c_{t+1}, l_{t+1}).$$

**Household's FOC for labor:**

$$- u_l(c_t, l_t) = \frac{1 - \tau_{l,t}}{1 + \tau_{c,t}} w_t u_c(c_t, l_t).$$

- Capital tax  $\tau_{k,t+1}$  depresses after-tax return to saving  $\Rightarrow$  less capital accumulation, lower growth.
- Labor tax  $\tau_{l,t}$  lowers after-tax wage  $\Rightarrow$  discourages work effort.
- Consumption tax  $\tau_{c,t}$  also distorts both saving and labor decisions.



# Long-Run Distortions (Steady State)

Assume constant tax rates and a standard Cobb-Douglas  $f(k, l) = k^\alpha l^{1-\alpha}$ .

- Steady state capital satisfies

$$1 = \beta [1 + (1 - \tau_k)(r - \delta)], \quad \text{where } r = \alpha k^{\alpha-1} l^{1-\alpha}.$$

- Higher  $\tau_k$  implies lower  $k$  in steady state and higher  $r$ .
- In GHH-type preferences (no income effect), labor depends negatively on both  $\tau_l$  and  $\tau_k$  (through wages).
- Overall, higher distortionary taxes reduce output below the efficient (planner) level.



# Tax Incidence in a Worker-Capitalist Economy

- Split agents into *workers* (own labor, no capital) and *capitalists* (own capital, no labor).
- Labor tax  $\tau_l$  directly affects workers' consumption; capital tax  $\tau_k$  directly hits capitalists. But *all* taxes affect equilibrium wages and rental rates, hence indirect effects on both groups.
- A key question: *Which types of taxes can raise how much revenue, and at what distortionary cost?*



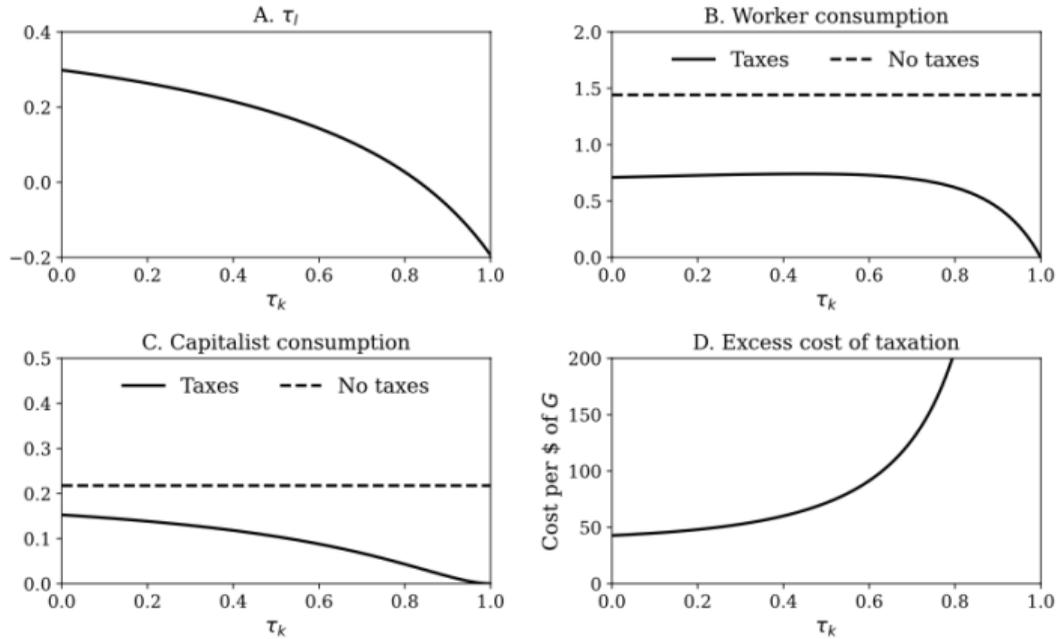


Figure 15.6: How Allocations Vary with  $\tau_k$ .



# Excess Cost of Taxation

- The **excess burden** or **deadweight loss** of taxes is how much private consumption falls per dollar of government revenue raised.
- Simulations often reveal that **capital taxes** can be especially distortionary in the long run (discouraging capital accumulation), leading to potentially large deadweight losses.
- But short-run and transition effects matter too.



# Tax Reform Example: Cutting Capital Taxes to Zero

- A known result: In the steady state, a **zero capital tax** ( $\tau_k = 0$ ) can be optimal (in a variety of models).
- **But:** Eliminating  $\tau_k$  might require *raising*  $\tau_l$ , which can *hurt* workers, especially in the short run.
- The **transition** may involve higher investment, lower consumption in the near term, and a slow buildup of capital. Long-run efficiency can rise, but short-run costs can be significant.
- *Distributional impacts:* capitalists gain immediately, workers face higher labor taxes. Final welfare effect depends on details (e.g., whether  $G$  is valued by all, etc.).



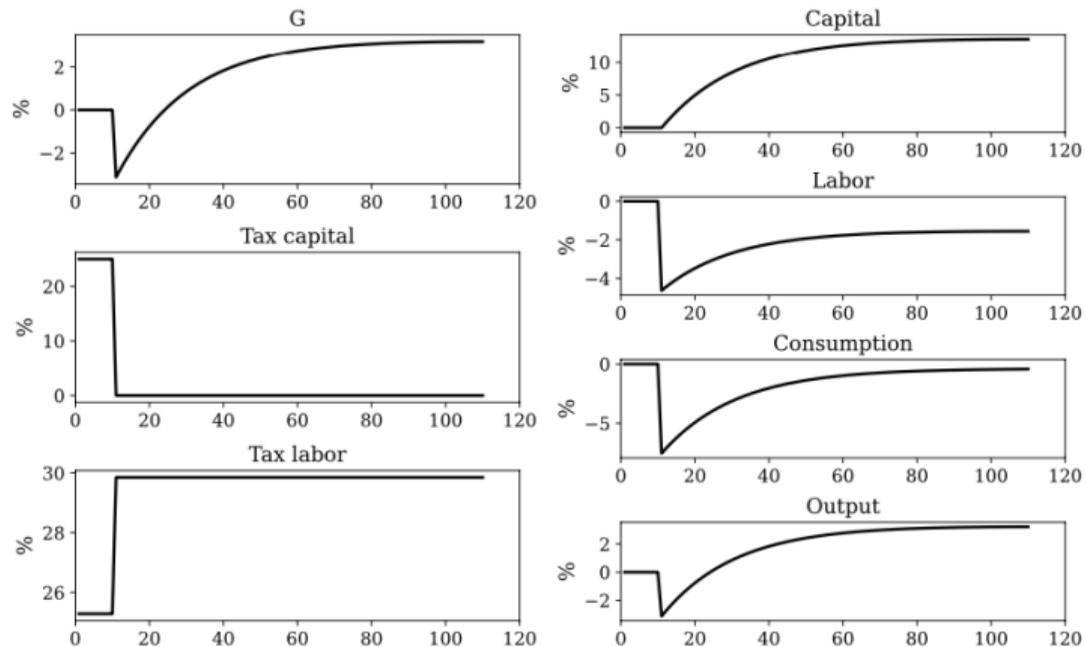


Figure 15.7: Eliminating capital income taxes.



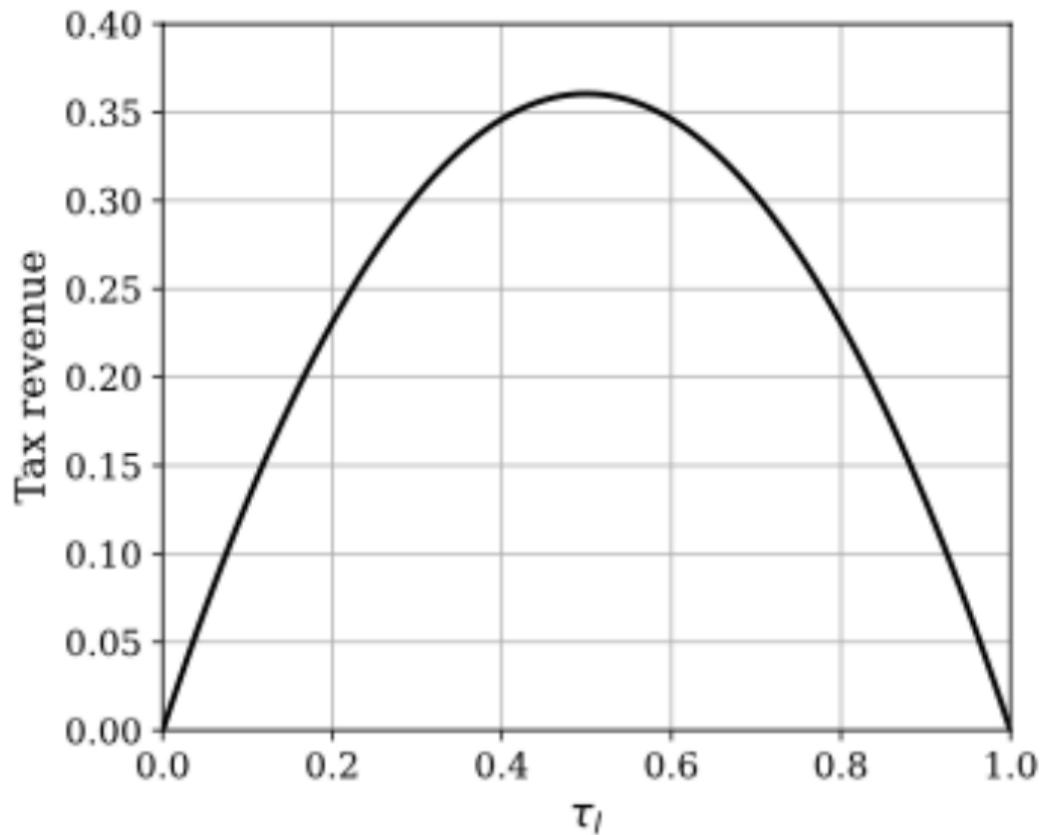
# Laffer Curve

- **Laffer curve:** relationship between tax rate and total *tax revenue*.
- Often hump-shaped:

$$\text{Revenue}(\tau_l) = \tau_l \cdot (\text{tax base})(\tau_l).$$

- As  $\tau_l \rightarrow 1$ , labor supply collapses, so revenue  $\rightarrow 0$ .
- Tax rate that *maximizes* revenue is not necessarily the same that maximizes *welfare*.





# Public Goods and Public Capital

- So far, we treated  $G_t$  as exogenous or “thrown into the ocean.”
- In reality,  $G_t$  can represent valuable **public goods** in utility:

$$u(c_t, g_t), \quad \text{with } g_t \text{ provided by the government.}$$

- Or **public investment**  $k_{g,t}$  in infrastructure (roads, schools):

$$y_t = f(k_t, l_t, k_{g,t}), \quad k_{g,t+1} = i_{g,t} + (1 - \delta_g) k_{g,t}.$$

- Optimal policy would weigh marginal benefit of public vs. private capital, net of depreciation.



# Debt Irrelevance with Lump-Sum Taxes

- **Ricardian Equivalence:** If taxes are lump-sum, the timing of taxes vs. debt is irrelevant for consumption and labor.
- Example: A two-period model with a representative household. A tax cut today financed by new govt debt implies higher taxes tomorrow, leaving the household's lifetime budget constraint the same.
- Households save the exact amount needed to pay future tax. No effect on real allocations or interest rates.



# When Ricardian Equivalence Fails

- **Distortionary taxes:** Timing *does* matter (e.g., capital vs. labor taxes).
- **Heterogeneity:** Some agents credit-constrained, or different generations (overlapping generations).
- **Finite lifetimes or incomplete markets:** May break the equivalence, as not all face the same future tax burdens.



# Ramsey Problem: Setup

## Key Idea:

- A **benevolent government** chooses *paths* of taxes  $(\tau_l, \tau_k, \dots)$  to maximize social welfare.
- Subject to resource constraints, equilibrium conditions, and no-lump-sum restriction.
- Typically yields two **classic** results in infinite-horizon settings:
  1. **Zero capital income tax** in the long run (Chamley-Judd).
  2. **Smooth labor taxes** over time (tax-smoothing).



# Ramsey in a Simple Two-Period Model

**Household:**

$$\max u(c_0, l_0) + \beta u(c_1, l_1).$$

Subject to:

$$c_0 = (1 - \tau_0) w_0 l_0 - b_0, \quad c_1 = (1 - \tau_1) w_1 l_1 + (1 + r(1 - \tau_{b,1})) b_0.$$

**Government:** finances  $g_0, g_1$  with  $\tau_0, \tau_1, \tau_{b,1}$ . Chooses to commit at  $t = 0$ .

**Result:**

- No capital tax in equilibrium,  $\tau_{b,1} = 0$  (if feasible).
- Constant labor tax rate  $\tau_0 = \tau_1 =$  “tax smoothing.”



# Time Inconsistency

- If the government *cannot commit* to future policies:
  - Ex post, it's tempting to heavily tax capital once it's installed (a lump-sum in the short run).
  - This leads to *time-inconsistent* plans: the government would deviate from the Ramsey plan if it could re-optimize in period 1.
- Institutional constraints or reputational mechanisms may help sustain commitment.
- Alternatively, *time-consistent* policy design has become an active research area.



# PAYG Pensions as Government Debt

Two-Period OLG Model with population growth  $n$ :

$$N_t = (1 + n)^t.$$

- Only the young work, endowment grows at rate  $\gamma$ :  $y_t = (1 + \gamma)^t \bar{y}$ .
- Government runs a **Pay-As-You-Go** (PAYG) pension:  $p_t$  to old, financed by tax  $\tau_p$  on the young's labor.
- Also finances **public good**  $G_t = g Y_t$  and possibly issues debt  $B_t$ .

$$p_t = (1 + n) \tau_p y_t.$$



# Why Ricardian Equivalence May Fail in OLG

- **Different cohorts** exist simultaneously:
  - Shifting taxes from the current young to future young is *not* neutral because they are different people.
- Debt-financed tax cut for current young implies higher taxes for future young.
- Overlapping generations  $\implies$  **timing of taxes** matters for distribution and macro aggregates.



# Returns in a PAYG System

- A PAYG system effectively yields a rate of return  $n + \gamma$  if each generation invests “contributions” and obtains “benefits” in old age.
- If  $r > n + \gamma$ , then forced contributions have lower return than private saving  $\Rightarrow$  future generations may be worse off under a PAYG expansion.
- If  $r < n + \gamma$  (dynamic inefficiency), a PAYG system can *raise* welfare for *all* generations.



# Tax Progressivity and Inequality

- U.S. tax/transfer system is often approximated by

$$y - T(y) = \lambda y^{1-\tau},$$

where  $\tau > 0$  indicates progressivity (higher marginal tax rates at higher incomes).

- The net result: the after-tax income distribution is *compressed* relative to pre-tax distribution.
- *Trade-off*: Higher progressivity can reduce inequality but can also reduce incentives (labor, investment).



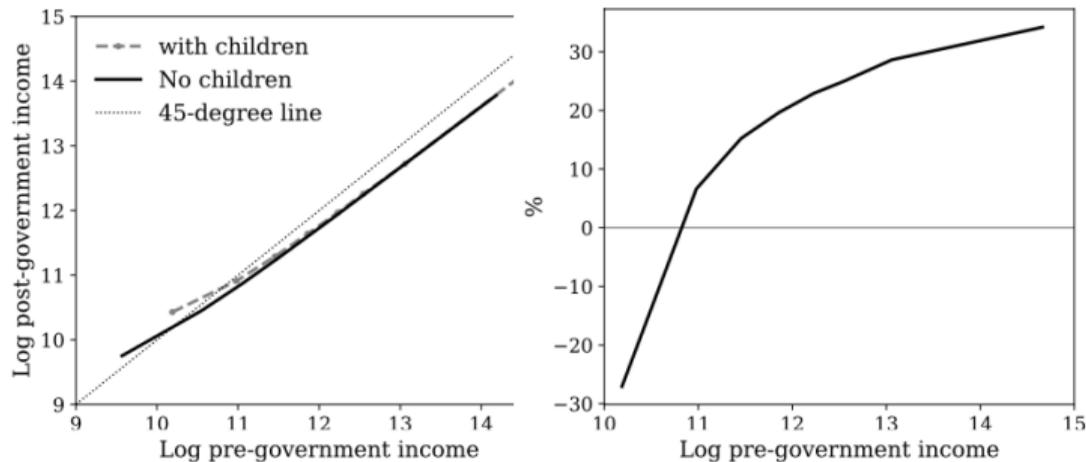


Figure 15.9: Left plot: Scatter plot of pre-government income against and post-government income for percentiles of U.S. households. Right plot: Average net tax rates by household income, defined as taxes minus transfers as a share of income, for households with children.

# A Simple Static Model of Progressivity

$$\text{Utility: } u(c_i, l_i) = \ln(c_i) - \frac{l_i^{1+1/\phi}}{1 + \frac{1}{\phi}}, \quad i \in [0, 1].$$

- Individuals differ in productivity  $w_i$ .
- Disposable income:  $c_i = \lambda (w_i l_i)^{1-\tau}$ .
- **Equilibrium results:**
  - Hours chosen to balance marginal benefit vs. net-of-tax wage. Certain preferences imply  $l_i$  is the same across  $i$  or might vary; typically progressivity  $\tau$  reduces average labor supply.
  - Consumption inequality dampened if  $\tau > 0$  since  $c_i \propto w_i^{1-\tau}$ .



# Key Trade-Off: Equity vs. Efficiency

- More progressive taxes  $\Rightarrow$  more **redistribution**, less disposable-income inequality.
- But also  $\Rightarrow$  **higher distortions**: lower labor supply, reduced capital accumulation in dynamic settings, etc.
- Policymakers weigh these pros and cons when designing tax/transfer systems.



# Chapter Conclusions

- Fiscal policy (taxes, spending, debt) has **deep implications** for efficiency and distribution.
- **Distortionary taxes** shape labor supply, savings, investment decisions.
- **Debt** policy: timing and composition of taxes, *tax smoothing*, potential *time inconsistency*.
- In **OLG** settings, debt and pensions alter intergenerational distribution (Ricardian Equivalence may not hold).
- **Redistribution** is central: progressive taxation can reduce inequality but may dampen incentives.



## Further Reading

- (Chamley, 1986) *Optimal Taxation of Capital Income in General Equilibrium with Infinite Lives*, *Econometrica*.
- (Judd, 1985). *Redistributive Taxation in a Simple Perfect Foresight Model*, *Journal of Public Economics*.
- (Barro, 1979) *On the Determination of Public Debt*, *Journal of Political Economy*.
- (Lucas and Stokey, 1983) *Optimal Fiscal and Monetary Policy in an Economy without Capital*, *Journal of Monetary Economics*.
- (Heathcote et al., 2017) *Optimal Tax Progressivity: An Analytical Framework*, *QJE*.



## References to Data (U.S. Focus)

- **Bureau of Economic Analysis (BEA)**, NIPA Tables 3.1, 3.16, etc.
- **Flow of Funds** (Federal Reserve) for debt series.
- **OECD** dataset for cross-country comparisons of government spending.
- **CBO** for household-level data on pre-/post-government income and average tax rates.



# References I

- Barro, R. J. (1979). On the determination of public debt. *Journal of Political Economy*, 82(6):1095–1117.
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# Thank you!

Questions or comments?

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