

# Chapter 19: Credit Market Frictions

## Graduate Macroeconomics Slides

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# Outline

- Introduction and Motivation
- Empirical Motivation
- Modeling Financial Frictions
- Financial Frictions in the Neoclassical Model
- A Two-Period Illustration
- Amplification via the Price of Capital
- Working Capital Requirements
- Numerical Example
- Critical Analysis
- Conclusion



# Motivation

- The 2008 financial crisis exposed limitations in mainstream macroeconomic models that assumed frictionless financial markets.
- Notable papers including (Bernanke and Gertler, 1989) and (Kiyotaki and Moore, 1997) highlighted the impact of financial (credit) frictions on macroeconomic dynamics.
- Historically, the role of financial markets in major events such as the Great Depression (e.g., (Calomiris, 1993), (Bernanke, 2024)) was sometimes underemphasized.
- This chapter incorporates financial frictions into a standard neoclassical growth framework and examines their macroeconomic implications.



# Key Questions

- Why do real and financial variables co-move so strongly over the business cycle?
- Are financial frictions simply propagating real shocks or can they themselves be a *source* of macroeconomic fluctuations?
- How can we model these frictions in an analytically tractable but empirically relevant way?

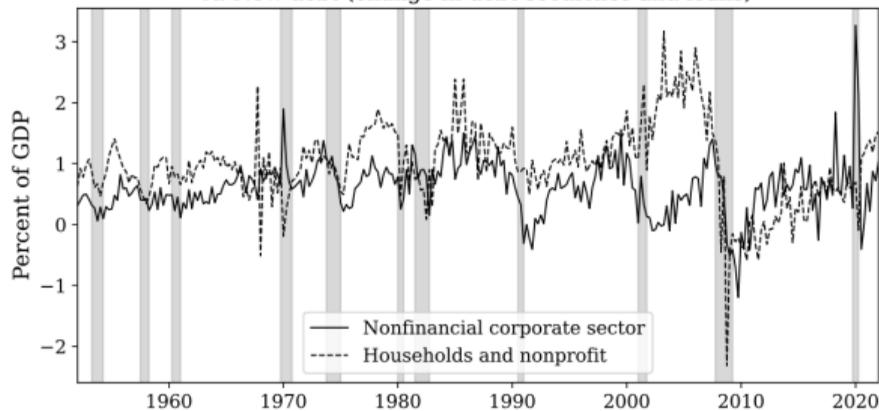


# Pro-Cyclical Credit Flows

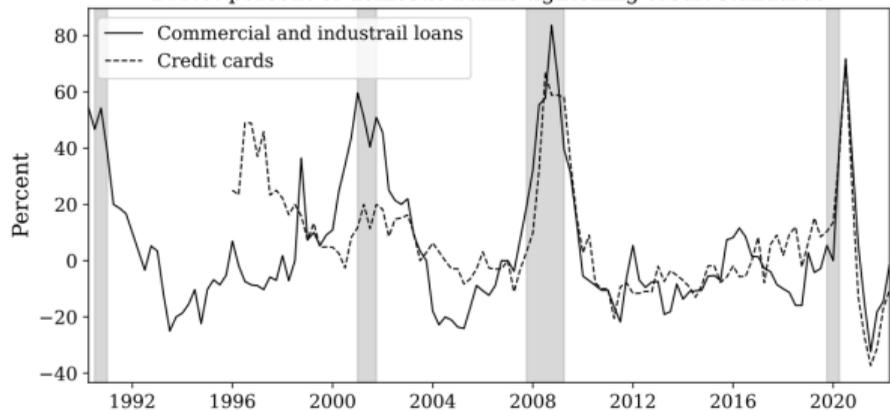
- Credit market liabilities (both household and business sector) typically expand during economic expansions and contract during recessions.
- **Figure 19.1 (Panel A):**
  - Growth of household and business debt in the US strongly correlates with GDP growth.
  - 2008 crisis saw a sharp drop in credit growth.
- **Figure 19.1 (Panel B):**
  - Bank loan officers report *tightening* of credit standards in recessions.
  - Lending *conditions* vary in a pro-cyclical manner.



A. New debt (change in debt securities and loans)



B. Net percent of domestic banks tightening credit standards



# Credit Spreads and Unemployment

- **Figure 19.2 (Panel A):**
  - Corporate bond spreads (Baa vs. Treasury) rise prior to recessions.
  - Reflects risk re-pricing and perceived borrower risk.
- **Figure 19.2 (Panel B):**
  - Negative co-movement between new private-sector debt and unemployment rate.
  - Strengthens the case that tighter credit is associated with rising unemployment.



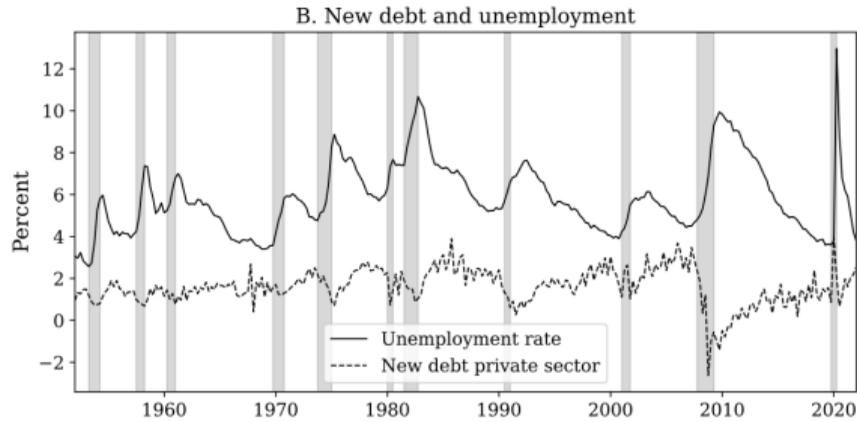
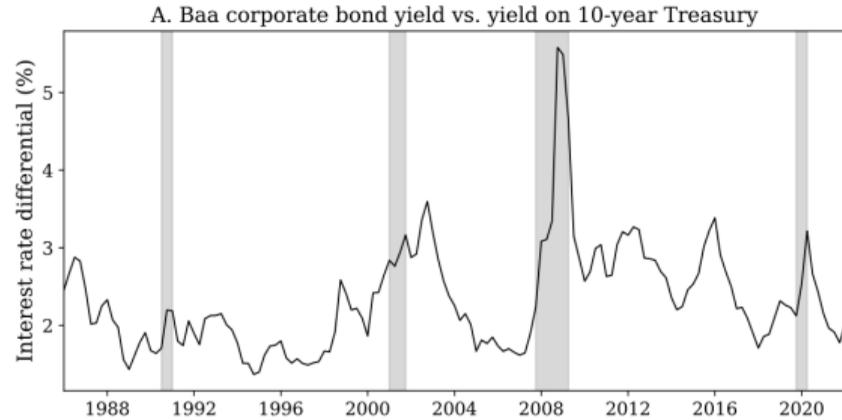


Figure 19.2: **Panel A:** Interest rate differential between U.S. corporate

## Three scenarios for real-financial interactions:

### 1. Real activity causes changes in credit flows.

- Recession leads to lower consumption/investment, hence less borrowing.

### 2. Financial frictions propagate non-financial shocks.

- E.g., a negative productivity shock erodes collateral, lowering credit capacity.
- Amplifies or dampens initial shocks.

### 3. Financial shocks as a direct source of fluctuations.

- Restrictive credit markets induce cutbacks in real activity.

*This chapter focuses on modeling frameworks for capturing cases (2) and (3).*



# What Are Financial Frictions?

- **Definition:** Costs, constraints, or missing markets limiting the ability of agents to borrow, lend, or insure against risks.
- **Necessary conditions:**
  1. Some markets are *incomplete* or missing.
  2. Agents differ in some dimension (*heterogeneity*) that creates the need to trade.
- If markets were complete, Modigliani-Miller irrelevance results would apply, rendering the source of financing unimportant to real decisions.



# Types of Market Incompleteness

## Exogenous Incompleteness

- Assumption: Only non-contingent debt is available (fixed repayment).
- Often implemented by placing an *exogenous borrowing limit*.

## Endogenous Incompleteness

- Financial contracts are limited by incentive constraints (information asymmetry, moral hazard, limited enforcement).
- E.g., (Bernanke and Gertler, 1989) (costly state verification), (Kiyotaki and Moore, 1997) (limited enforcement with collateral).



# Heterogeneity and Self-Financing

- **Heterogeneous Agents:** Borrowers vs. lenders, high vs. low productivity, different discount factors, etc.
- Borrowing constraints matter if some agents are persistently constrained.
- Mechanisms preventing *self-financing*:
  - Finite horizons or overlapping generations.
  - Differing levels of *time preference*.
  - Tax benefits of debt or “convenience yields.”
- Common outcome: Constrained agents maintain high leverage; unconstrained agents are net lenders.



# Baseline Neoclassical Framework

- Representative household with preferences:

$$\sum_{t=0}^{\infty} \beta^t u(C_t, L_t).$$

- Firms produce using a production function  $F(K_t, L_t)$  and accumulate capital.
- In the *complete markets* case, the source of funding (debt vs. equity) is irrelevant (Modigliani-Miller).
- We now *break* this irrelevance by introducing:
  1. A **tax advantage** to debt.
  2. A **borrowing limit** (collateral constraint).
  3. A **dividend adjustment cost**.



# Firm Optimization with Frictions

Firm faces:

$$\max_{\{d_t, k_{t+1}, b_{t+1}, l_t\}} \sum_{t=0}^{\infty} m_t d_t$$

Subject to:

Budget Constraint:

$$F(z_t, k_t, l_t) - w_t l_t + \frac{b_{t+1}}{R_t} \\ = b_t + k_{t+1} - (1 - \delta)k_t + \varphi(d_t),$$

Borrowing Constraint:

$$\frac{b_{t+1}}{\tilde{R}_t} \leq \xi p_t k_{t+1},$$

$$\varphi(d_t) = d_t + \kappa (d_t - \phi)^2,$$

where  $\tilde{R}_t = \frac{R_t}{(1+\tau)}$  represents the effective interest cost.



# Interpretation of Constraints

- **Tax Advantage ( $\tau$ ):**

$$\tilde{R}_t = \frac{R_t}{1 + \tau}, \quad \tau > 0 \implies \tilde{R}_t < R_t.$$

- **Collateral Constraint ( $\xi p_t k_{t+1}$ ):**

- Firms can borrow only a fraction  $\xi$  of the next period capital's market value  $p_t k_{t+1}$ .
- Captures limited enforcement or secured borrowing with capital as collateral.

- **Dividend Adjustment Cost ( $\kappa$ ):**

- Raising equity or significantly cutting dividends is costly.
- Creates a *pecking order* favoring debt over equity but *discouraging* large changes in dividend policies.



# First-Order Conditions

- Labor:

$$F_L(z_t, k_t, l_t) = w_t.$$

- Capital:

Expected Return = Effective Cost – (Collateral Value Term),

$$\underbrace{E_t[m_{t+1} (F_K(z_{t+1}, k_{t+1}, l_{t+1}) + (1 - \delta))]}_{\text{discounted MPK+resale}} = \underbrace{(1 + \mu_t \xi)}_{\text{wedge}} p_t,$$

where  $\mu_t$  is the multiplier on the borrowing constraint.

- Debt:

$$(1 - \mu_t)(1 + \tau) = \frac{1}{E_t[m_{t+1}]},$$

in a simplified setup. If  $\tau > 0$ , the constraint tends to bind ( $\mu_t > 0$ ).



# Two-Period Model Setup

- Periods  $t = 0, 1$  with no uncertainty (for simplicity).
- Period 0: Firms choose  $k_1, b_1, l_0, d_0$  subject to constraints.
- Period 1: Production occurs with  $F(z_1, k_1, l_1)$  and all capital is consumed or scrapped ( $k_2 = 0$ ).
- Collateral constraint:

$$\frac{b_1}{(1 + \tau)} \leq \xi p k_1.$$

- Dividend cost:

$$\varphi(d_0) = d_0 + \kappa (d_0 - \phi)^2.$$



# Insights from the Two-Period Model

- **Positive Productivity Shock** ( $z_0, z_1$  both increase):
  - Firms desire to invest more in  $k_1$ .
  - Must partly rely on *equity* (cut current dividends), raising the cost of investing.
  - $\implies$  **Investment can be dampened** compared to frictionless case.
- **Financial Shock** ( $\xi$  changes):
  - Tighter constraint ( $\downarrow \xi$ ) reduces  $k_1$  and next period output.
  - Relaxed constraint ( $\uparrow \xi$ ) *may or may not* increase  $k_1$  substantially, as firms might not fully utilize new borrowing capacity (precaution or costs of large dividend changes).



# Asymmetric Effects of Financial Shocks

- **Positive shock:**  $\xi \uparrow$ 
  - If previously unconstrained, no change in borrowing or investment.
  - If previously constrained, can expand credit and investment (but possibly gradually).
- **Negative shock:**  $\xi \downarrow$ 
  - If previously unconstrained, might remain unconstrained unless shock is large.
  - If constrained, forced to reduce debt (big drop in  $k_1$  or dividends).
  - $\implies$  Potentially sharper real contraction than the expansion in the positive-shock scenario.



# Role of Asset Prices

- In many models ((Bernanke et al., 1999), (Kiyotaki and Moore, 1997)),  $p_t$  (price of capital) rises in expansions and falls in contractions.
- Changes in  $p_t$  affect collateral value  $\xi p_t k_{t+1}$ :
  - **Boom:** Higher  $p_t \implies$  easier borrowing, reinforcing capital accumulation (a *positive feedback loop*).
  - **Bust:** Lower  $p_t \implies$  net worth collapses faster, reducing borrowing capacity and forcing deeper cuts.
- This *financial accelerator* mechanism is key to understanding “amplified” business cycles.



# Working Capital Constraint

- Firms may need to finance **wage payments** in advance:

$$w_t l_t + \frac{b_{t+1}}{R_t} \leq \xi p_t k_{t+1}.$$

- This *directly* links credit constraints to labor demand:

$$F_L(z_t, k_t, l_t) = (1 + \mu_t) w_t \quad (\text{if binding}).$$

- Tighter constraints  $\implies \mu_t > 0 \implies$  effective *markup* on  $w_t$ , reducing labor demand and output.
- $\implies$  Credit frictions matter not only for investment but also for **employment** fluctuations.



# Calibration Overview

- Quarterly model with standard RBC parameters:

$$\beta = 0.983, \quad \alpha = 0.36, \quad \text{etc.}$$

- $\tau = 0.281$ : approximate effective corporate tax rate in the US.
- $\kappa$ : chosen to match empirical volatility of dividend payouts.
- $\xi$ : follows a Markov chain capturing variation in borrowing limits, matched to average corporate debt-to-capital ratio and its volatility.
- Productivity  $z_t$ : also Markov, matched to RBC Solow residual persistence and volatility.



# Simulation Results: Productivity Shock

*Stylized simulation: A persistent positive productivity shock at time 0.*

- Debt, output, and labor move together, but the multiplier  $\mu_t$  drops in the boom (less tight credit).
- Result: Procyclical debt and output, consistent with data patterns.



# Simulation Results: Financial Shock

*Stylized simulation: An increase vs. decrease in  $\xi$ .*

- Positive shock ( $\xi \uparrow$ ): Modest credit expansion and moderate output growth.
- Negative shock ( $\xi \downarrow$ ): Sharp contraction in credit  $\implies$  large drop in output.
- Asymmetry arises from precautionary and/or binding constraints.



Table 19.1: Parameter values.

Parameters	Description	Values
$\beta$	Discount factor	0.983
$\nu$	Utility parameter	0.412
$\alpha$	Capital share in production	0.360
$\tau$	Benefit of debt	0.281
$\kappa$	Dividends' cost	0.500
$p$	Price of capital	1.000
$z$	Productivity and transition probabilities	$\begin{pmatrix} 0.183 \\ 0.185 \\ 0.187 \end{pmatrix}, \begin{bmatrix} 0.900 & 0.075 & 0.025 \\ 0.050 & 0.900 & 0.050 \\ 0.025 & 0.075 & 0.900 \end{bmatrix}$
$\xi$	Debt limit and transition probabilities	$\begin{pmatrix} 0.450 \\ 0.500 \\ 0.550 \end{pmatrix}, \begin{bmatrix} 0.900 & 0.075 & 0.025 \\ 0.050 & 0.900 & 0.050 \\ 0.025 & 0.075 & 0.900 \end{bmatrix}$



## Simulation Exercise

- The economy is hit by two exogenous processes: a productivity level  $z \in \{0.183, 0.185, 0.187\}$  and a financial tightness variable  $\xi \in \{0.450, 0.500, 0.550\}$ , with agents forming expectations from the Markov structure.
- We start from the stochastic steady state at the mean realizations  $(z, \xi) = (0.185, 0.500)$ , and at  $t=0$  we engineer one discrete “switch” to study dynamic responses.
- Borrowing is subject to a constraint with Lagrange multiplier  $\mu_t \geq 0$ ; the constraint is binding throughout the productivity experiments ( $\mu_t > 0$  at all  $t$ ).
- Two counterfactuals are run: (i) a productivity boom  $z : 0.185 \rightarrow 0.187$  (and symmetrically a contraction  $z : 0.185 \rightarrow 0.183$ ) holding  $\xi = 0.500$ , and (ii) a credit boom  $\xi : 0.500 \rightarrow 0.550$  (and symmetrically a tightening  $\xi : 0.500 \rightarrow 0.450$ ) holding  $z = 0.185$ .



# Productivity shocks: dynamic responses and facts

- A positive productivity switch raises output immediately and persistently, while debt rises only modestly; the mirror image holds for a negative switch.
- The multiplier  $\mu_t$  moves countercyclically with productivity: it falls in booms and rises in contractions, which is consistent with countercyclical credit spreads and tighter lending standards in downturns (cf. the facts summarized around their Figs. 19.1–19.2).
- The small debt response relative to output contrasts with the data, where debt often moves more than activity; this gap highlights the importance of financial shocks for matching credit facts.



# Productivity switch

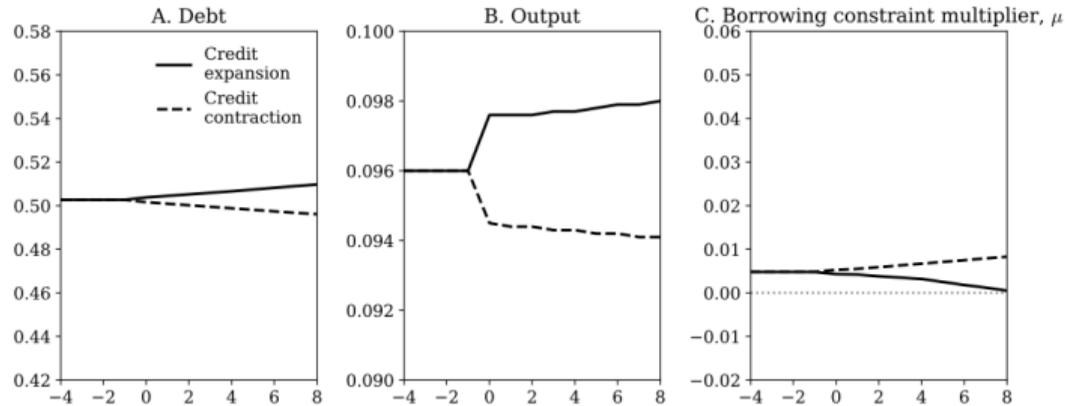


Figure 19.3: Response of debt, output, and borrowing constraint multiplier to a persistent productivity shock.



# Financial shocks: asymmetric quantity and tightness effects

- A positive financial shock (credit expansion  $\xi: 0.500 \rightarrow 0.550$ ) generates a gradual and persistent increase in debt with only a mild, hump-shaped rise in output.
- A negative financial shock (credit tightening  $\xi: 0.500 \rightarrow 0.450$ ) induces a sharp fall in debt and a large, abrupt output contraction that is not very persistent.
- After a credit expansion the constraint becomes slack ( $\mu_t \rightarrow 0$ ), whereas after a tightening  $\mu_t$  spikes, tracking the surge in effective financial tightness.



# Financial switch

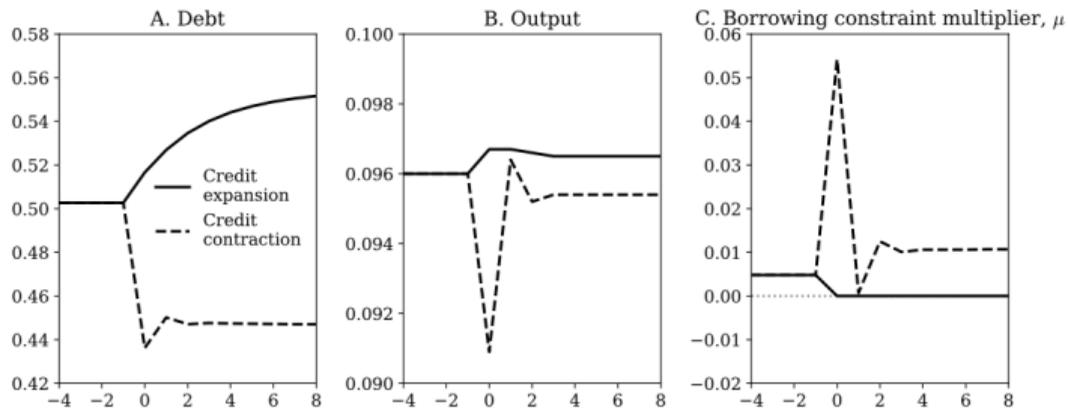


Figure 19.4: Response of debt, output, and borrowing constraint multiplier to a persistent financial shock.



# Mechanism for the asymmetry

- When  $\xi$  jumps up, firms anticipate the possibility of reversal, so the shadow value of relaxing the constraint tomorrow implies a *precautionary* motive not to immediately hit the new limit; formally, the Euler equation for liabilities weighs  $U_{c,t}$  against  $U_{c,t+1}$  under a binding-constraint wedge  $\mu_t$ .
- When  $\xi$  falls, the constraint tightens and firms must restore feasibility either by reducing labor and investment (to shrink external financing needs) or by raising equity via lower dividends; both margins are costly, so the optimal combination causes a large, sudden drop in debt and output.
- In the productivity experiments the constraint remains binding ( $\mu_t > 0$ ), which keeps debt co-moving with output but with a smaller amplitude because the effective borrowing limit does not relax.



## External validation and key takeaways

- The simulated credit dynamics match broad empirical regularities: credit booms are not necessarily paired with outsized real growth, while sudden credit stops produce sharp contractions (Reinhart and Rogoff, 2009; Schularick and Taylor, 2012).
- The model reproduces procyclical debt and countercyclical measures of financial tightness (spreads, lending standards  $\leftrightarrow \mu_t$ ).
- **Bottom line:** Productivity shocks mainly move output, whereas financial shocks mainly move debt and do so *asymmetrically*; capturing this asymmetry is crucial for business-cycle credit facts and for policy counterfactuals.



# Discussion Points

- **Amplification vs. Dampening:**
  - If equity issuance is still viable (albeit costly), frictions can *dampen* or *amplify* shocks depending on model specifics.
- **Big Role for Asset Prices:**
  - Endogenous  $p_t$  typically creates stronger amplification (financial accelerator).
- **Labor Wedge with Working Capital:**
  - Tighter credit directly reduces labor demand, making financial frictions more potent for output fluctuations.
- **Asymmetry in Booms vs. Busts:**
  - Credit expansions might be gradual, but reversals can be abrupt and severe.



# Policy Implications

- **Macroprudential Policy:**
  - Limiting excessive leverage during expansions to prevent sharp busts.
- **Lender of Last Resort / Unconventional Monetary Policy:**
  - Easing credit constraints in crises to mitigate adverse feedback loops.
- **Tax Policy:**
  - Debt bias in corporate tax codes can affect average leverage, influencing how frequently constraints bind.



# Conclusion

- Financial market frictions are **non-negligible** and can significantly shape macroeconomic dynamics.
- They can generate procyclical credit flows, amplify or dampen shocks, and produce sharp recessions upon negative credit events.
- Key elements:
  - Collateral constraints,
  - Debt-equity wedges,
  - Working capital requirements.
- Extending the *standard* neoclassical model with simple financial frictions captures many qualitative stylized facts of modern financial crises.



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# Thank you!

Questions or comments?

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