

Chapter 25: Sustainability

Graduate Macroeconomics Slides

Orhan Torul

Boğaziçi University

January 23, 2026



Outline

- Introduction
- The Economy and the Environment
- Climate Change: Natural-Science Background
- Integrated Assessment Models
 - A Static One-Region Model
 - A Fully Dynamic IAM
- Natural Resources in Finite Supply
 - Data and Trends
 - Basic Theory
 - Capital-Energy Complementarity
 - Taking Stock
- Summary and Final Remarks
- References



Motivation and Context

Key Issue: Climate Change as a Macroeconomic Challenge

- Climate change is global: *aggregate* CO₂ emissions matter.
- Fossil fuels remain central to energy use ($\sim 5\%$ of global GDP devoted to energy).
- Sharp reductions in energy use may cause large macroeconomic fluctuations (e.g., the 1970s oil-price shocks).
- Policymaking challenge: evaluating long-run policies with limited direct evidence.

Objective: Develop simple *macroeconomic* tools to assess climate policy impacts on the climate and on welfare.



What is Sustainability?

- **Broad concern:** Do humans – now and in the future – have enough resources for survival and well-being?
- **Focus:** Natural resources, climate, and how they intersect with economic growth.
- **Policy questions:**
 - How to manage finite natural resources?
 - Should we aim for *de-growth* to protect the environment?
 - Key trade-offs between preserving nature vs. promoting economic activity.
- This chapter: begin to address these questions using macro models and insights from public/environmental economics.



The Economy in a Broader Natural Context

- **Environment** in micro theory: preferences, technology, etc.
- Here: environment = *nature*.
- Movements to preserve the environment (especially in advanced economies).

Conceptual framework :

- The economy (*households, firms, government*) interacts with *land mass, finite resources, climate, water, biodiversity, solar energy*.
- Different degrees of property rights:
 - Land typically has stronger property rights.
 - Atmosphere/climate is a global public good → very limited property rights.



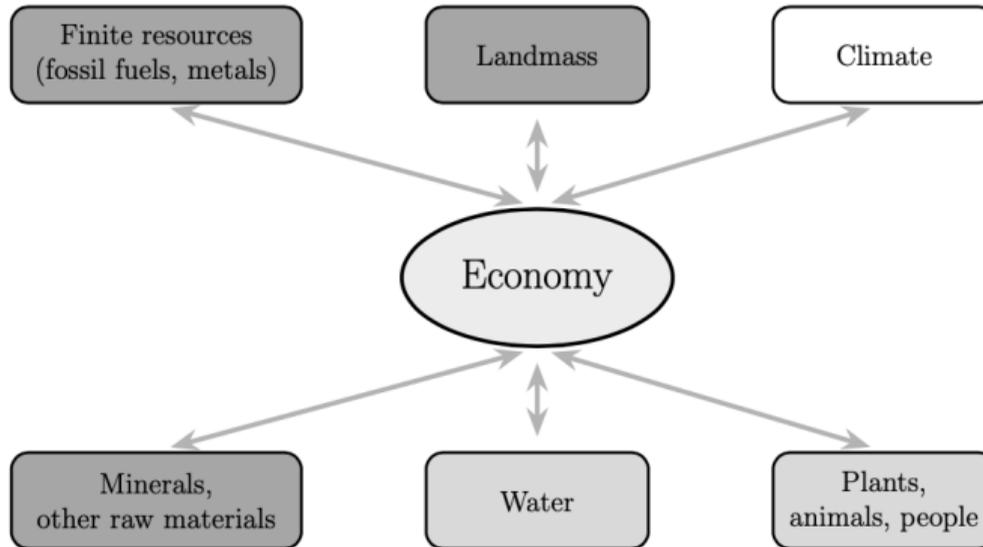


Figure 25.1: The economy and the environment. Darker shades of grey reflect a higher degree of property rights.

Integrated Assessment Models (IAMs)

- **IAM:** Integrates economy, carbon cycle, and climate module.
 1. *Economy:* Usually a growth model with fossil-fuel energy use → CO₂ emissions.
 2. *Carbon Cycle:* The pathway of CO₂ among atmosphere, land, and oceans.
 3. *Climate Module:* Models warming from CO₂ in the atmosphere, capturing greenhouse effects.
- **Damages:** Higher temperature → climate-related damages (storms, sea-level rise, etc.) → reduces economic output/utility.
- **Policy:** Negligible private cost to emit ⇒ negative externality. Proper *carbon pricing* or other policy recommended.



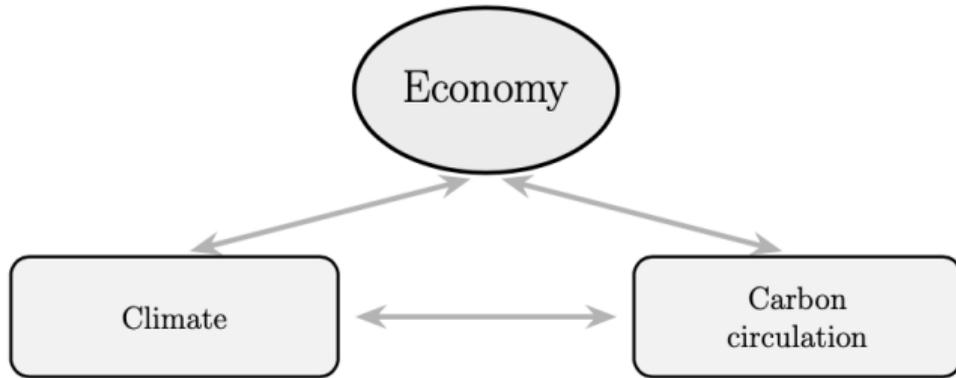


Figure 25.2: Integrated Assessment Models, IAMs, consist of three building blocks: an economy, a representation of the carbon cycle, and a climate module.

Greenhouse Effect: A Primer

Energy balance approach:

- Earth receives *solar radiation*, reflects some energy, emits heat.
- CO₂ *does not* affect incoming solar radiation but *does* impede outgoing heat radiation.
- CO₂ in atmosphere acts like a greenhouse: traps heat.
- Without the natural greenhouse effect, Earth would be -20°C ; currently $\sim 15^{\circ}\text{C}$.

Basic model:

$$\frac{dT(t)}{dt} = \sigma_1 \left(f(t) - \kappa T(t) \right),$$

where T is temperature deviation, f is *forcing*, and κ includes feedback effects (e.g., ice albedo).



Logarithmic Forcing of CO₂

- **Arrhenius greenhouse law:** forcing from CO₂ is proportional to $\ln(S/S_0)$.

$$f_{\text{CO}_2} = \eta \ln\left(\frac{S}{S_0}\right) / \ln(2),$$

where S_0 is pre-industrial CO₂ concentration.

- η/κ is the *equilibrium climate sensitivity* (ECS): expected long-run ΔT from doubling CO₂.
 - IPCC likely range: 2.5°C–4°C, with best estimate $\sim 3^\circ\text{C}$.
- Ocean heat absorption slows warming: multi-box energy-balance models often used (two-layer system for atmosphere/oceans).



Carbon Cycle

- **Three main reservoirs:**
 1. Atmosphere
 2. Surface ocean & biosphere
 3. Deep oceans
- CO₂ is emitted into atmosphere (E_t) and circulates among these reservoirs.
- Example (Nordhaus RICE model):

$$S_t - S_{t-1} = \phi_{12}S_{t-1} + \phi_{21}S_{t-1}^U + E_{t-1},$$

$$S_t^U - S_{t-1}^U = \phi_{12}S_{t-1} - (\phi_{21} + \phi_{23})S_{t-1}^U + \phi_{32}S_{t-1}^L,$$

$$S_t^L - S_{t-1}^L = \phi_{23}S_{t-1}^U + \phi_{32}S_{t-1}^L.$$

- **Key property:** A portion of CO₂ stays in atmosphere *for centuries* or longer.



Constant Carbon-Climate Response

- **Empirical finding:** ΔT is approximately **linear** in **cumulative** emissions.

$$T_t \approx \sigma_{\text{CCR}} \sum_{s=0}^t E_s, \quad (\text{carbon-climate response CCR})$$

- **Implications:**

- *Irreversibility* in warming: temperature remains elevated even if emissions go to zero.
 - *Carbon budget*: a desired temperature target implies a maximum total CO_2 that can be emitted.
 - Many emission paths can yield the same cumulative total, but differ in economic welfare outcomes.
- IPCC 6th report: TCRE range 1.0°C – 2.3°C per 1000 GtC (roughly 0.27 – 0.63 $^\circ\text{C}$ per Tt CO_2).



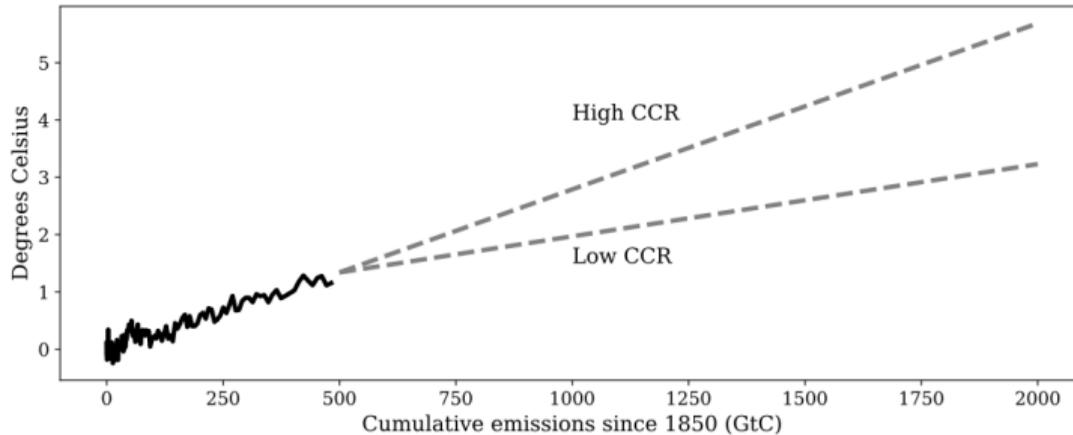


Figure 25.3: Cumulative carbon emissions and the global mean temperature. Solid line: historical data 1850-2022. Dashed lines: forecasts based on constant CCR.

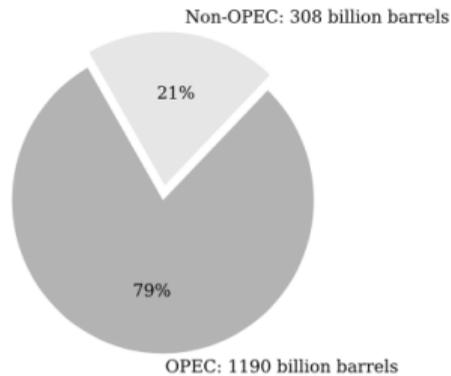


Fossil Energy Supply

- **Proven reserves vs. resources:**
 - *Reserves*: can be extracted profitably with current technology/prices.
 - *Resources*: total amount in discovered+undiscovered deposits, not necessarily profitable now.
- **Example (Oil):**
 - OPEC holds $\sim 80\%$ of world crude reserves.
 - Unconventional vs. conventional oil: unconventional has much higher extraction cost.
- **Reserve sizes (in GtC or GtCO₂):**
 - Coal reserves: $\sim 2,759$ GtCO₂ (BP, 2021).
 - Oil reserves (OPEC): ~ 500 GtCO₂.



OPEC share of world crude oil reserves



Shares within OPEC

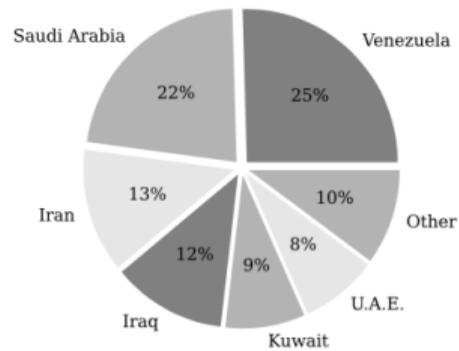


Figure 25.4: Oil Supply.

Source: OPEC (2019).



Table 25.1: Reserves and resources in GtC

	Reserves	Resources (Rogner)	Resources (BGR)
Oil (conv+unconv)	173	$\approx 400 - 2,200$	≈ 500
Coal	1,074	$\approx 6,200$	$\approx 11,500$
Gas	100	≈ 350	≈ 365

Sources: Rogner (1997), BGR (2020). BGR is the Federal Institute for Geosciences.

Figure: (Rogner, 1997), (BGR, 2020)



Damages

- **Economic perspective:** climate damages are negative externalities from emissions.
- **Valuation approaches:**
 1. Bottom-up: sum costs (agricultural losses, health impacts, sea-level rise, extreme events, etc.).
 2. Top-down: relate changes in output (GDP) or mortality to temperature changes (cross-section or panel).
- **Examples:**
 - **Stern Review (2007):** large estimated damage costs, motivating aggressive policy.
 - **Nordhaus DICE:** more modest damage estimates, $\sim 2.4\%$ of GDP lost at $+3^{\circ}\text{C}$.
- **Adaptation** offsets some damages (e.g., building sea walls, adopting new crop varieties).
- **Discounting debate:** market discount rates vs. ethical considerations for future generations.



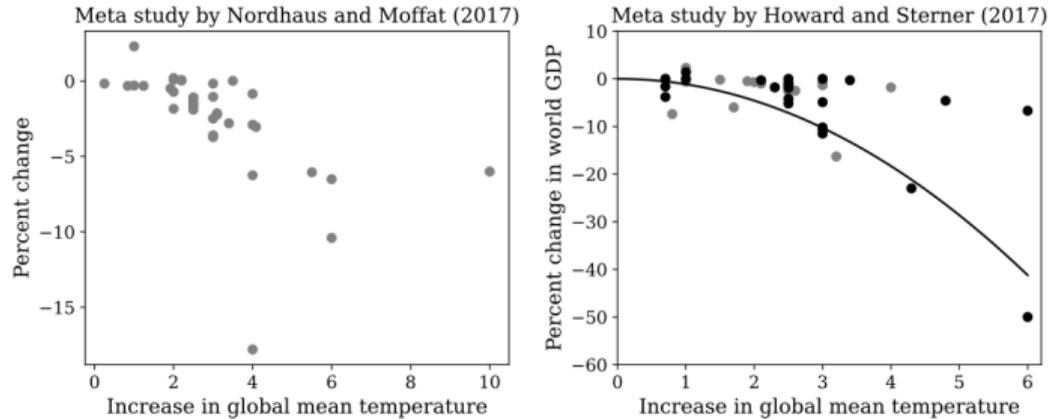


Figure 25.5: Meta studies of damages. Left: study by [Nordhaus and Moffat \(2017\)](#). Right: study by [Howard and Sterner \(2017\)](#) with black dots showing non-duplicate studies and the regression line preferred by those authors.

Figure: (Nordhaus and Moffat, 2017)



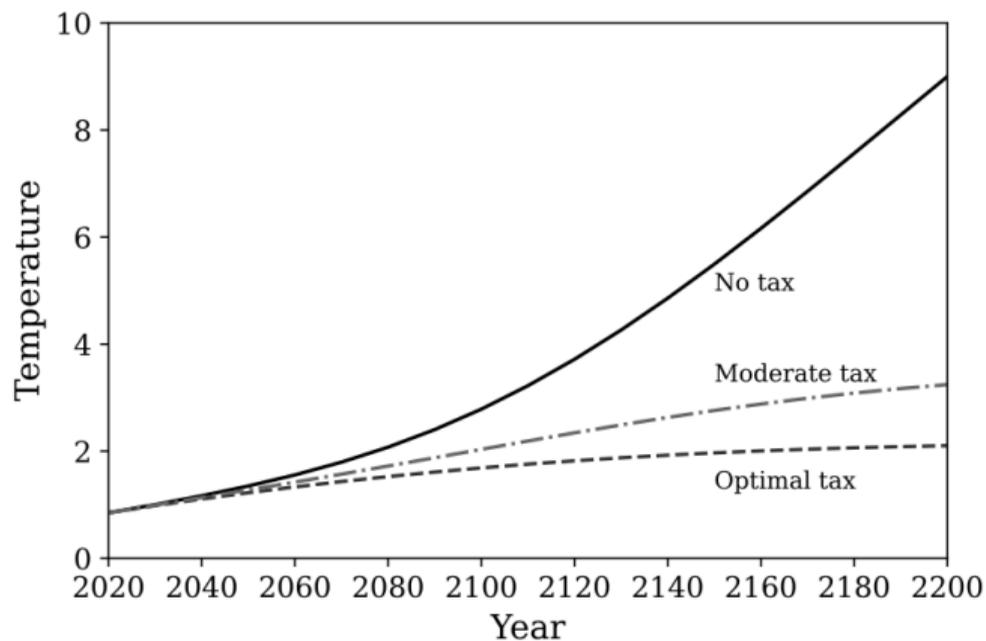


Figure 25.6: The effect on the global temperature of different carbon taxes.

Notes: The optimal tax is set to U.S. \$25 per ton CO₂ and the moderate tax is U.S. \$8 per ton CO₂.



Figure: (Howard and Sterner, 2017)

A Simple Static IAM

- **Sectors:**
 1. Final goods: uses capital, labor, and *energy services* in production.
 2. Energy services: produced from coal with cost p per unit.
- **Production:** $Y = AK^\alpha L^{1-\alpha-\nu} E^\nu$. In a simplified form, set $K = L = 1$, so $Y = AE^\nu$.
- **Damages:** $D(E) = \gamma E^2$.
- \Rightarrow **Consumption:** $C = AE^\nu - pE - \gamma E^2$.



Social Planner vs. Market Outcome

Market economy (private firm) solves:

$$\max_E AE^\nu - (p + \tau) E.$$

First-order condition: $\nu AE^{\nu-1} = p + \tau$.

Social planner internalizes damages:

$$\max_E AE^\nu - pE - \gamma E^2.$$

First-order condition: $\nu AE^{\nu-1} = p + 2\gamma E$.

- **Pigouvian Tax:** $\tau^* = 2\gamma E^*$.
- **Interpretation:** tax each unit of emissions by the *marginal damage* it imposes on society.



Prices vs. Quantities (Regulation)

- **Cap-and-trade (quantity restriction):**

- Government issues emissions permits up to \bar{E} .
- Market price of a permit: λ .
- If $\bar{E} = E^*$ (socially optimal), then $\lambda = 2\gamma E^*$.
- Price-based vs. quantity-based policy \Rightarrow *equivalent* in deterministic framework (Weitzman, 1974, with caveats).

- **Firm heterogeneity:**

- A single aggregate emissions limit \bar{E} still leads to cost-effective allocation if permits are tradable.



A Two-Region Model Setup

- **Regions:**

1. *Oil producer*: has finite stock R_t .
2. *Oil consumer*: invests in capital, uses labor, can import oil or use alternative energy.

- **Preferences:**

$$\sum_{t=0}^{\infty} \beta^t \ln(C_t).$$

- **Production function (oil-consuming region):**

$$Y_t = e^{z_t - \gamma S_t} K_t^\alpha L_t^{1-\alpha-\nu} E_t^\nu.$$

- Damages: factor productivity is $\exp(-\gamma S_t)$.
- S_t evolves with the **carbon cycle** plus emissions from oil/coal use.



Energy Aggregation and Resource Constraint

Three energy sources: oil (o), coal (c), green (g).

$$E_t = \left[\lambda_o e_{o,t}^\rho + \lambda_c e_{c,t}^\rho + \lambda_g e_{g,t}^\rho \right]^{1/\rho}.$$

Oil producer: stock R_t , evolves via

$$R_{t+1} = R_t - e_{o,t}, \quad R_0 = \bar{R}.$$

Market clearing in energy: price of oil $p_{o,t}$ determined by *equalizing supply/demand* each period, with no storage.

Household invests in capital and consumes:

$$C_t + K_{t+1} = Y_t - (p_{o,t}e_{o,t} + p_c e_{c,t} + p_g e_{g,t}).$$



Government, Emissions, and Policy

- **Carbon tax** τ_t on fossil use:

$\tau_t(e_{o,t} + e_{c,t})$ with proceeds rebated to consumers.

- **Emissions:**

$$M_t = e_{o,t} + e_{c,t} \quad (\text{in carbon units}).$$

- **Carbon cycle:**

$$S_{t+1} = S_t + (1 - \delta)M_t + \dots \quad (\text{e.g., see linear approximation or multi-box models}).$$

- **Dynamic** problem typically solved *numerically*, but with special functional forms (Cobb-Douglas in production, log utility), an almost closed-form solution emerges.



Marginal Damage and the Pigou Principle

- With $\ln(C)$ utility and exponential damage $\exp(-\gamma S)$:

$$\tau_t = \left(\text{Marginal Damage} \right) = Y_t \left[\gamma \sum_{j=0}^{\infty} \beta^j (1 - d_j) \right].$$

- $\tau_t \uparrow$ with:
 - higher γ (damage),
 - slower carbon decay $(1 - d_j)$,
 - lower discount rate β .
- **Key takeaway:** The optimal carbon tax depends on:
 1. The magnitude of damages (γ),
 2. The longevity of CO_2 in atmosphere,
 3. The social discount factor.



Simulation Example

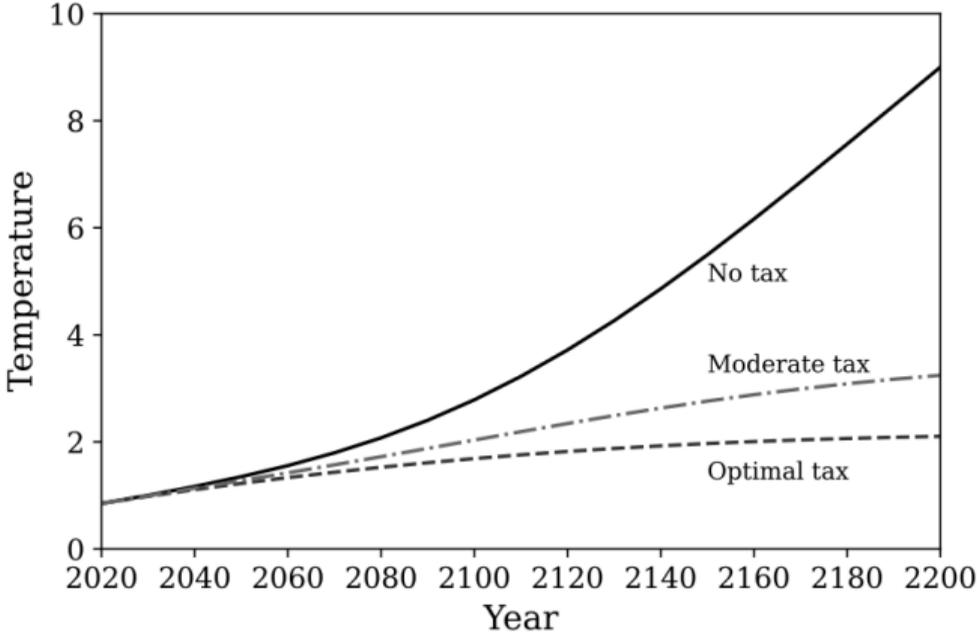


Figure 25.6: The effect on the global temperature of different carbon taxes.

Notes: The optimal tax is set to U.S. \$25 per ton CO₂ and the moderate tax is U.S. \$8 per ton CO₂.



Simulation Example cont'd

- **Calibration** (following [Golosov et al., 2014](#)):
 - Period = 10 years, $\alpha = 0.3$, $\nu = 0.05$, $\beta = (0.985)^{10}$, damage parameter γ from Nordhaus.
 - Initial oil stock, initial atmospheric carbon S_0 , etc.
- **Policy scenarios:**
 1. $\tau = 0$ (laissez-faire).
 2. $\tau = \tau^*$ (optimal).
 3. $\tau = \frac{1}{3}\tau^*$ (moderate).
- **Result:**
 - No policy: temperature could rise by 9°C by 2200.
 - Optimal $\tau \approx \$25/\text{ton CO}_2$: limit warming to $\approx 2^\circ\text{C}$.
 - Even moderate tax significantly reduces warming from the no-policy path.



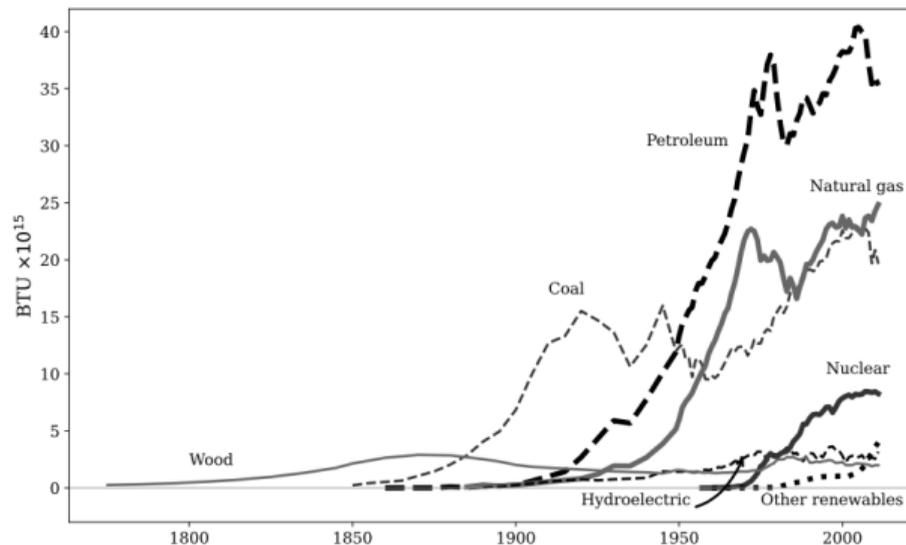


Figure 25.7: U.S. energy consumption.

Source: Administration (2012).

Figure: (Administration, 2012)



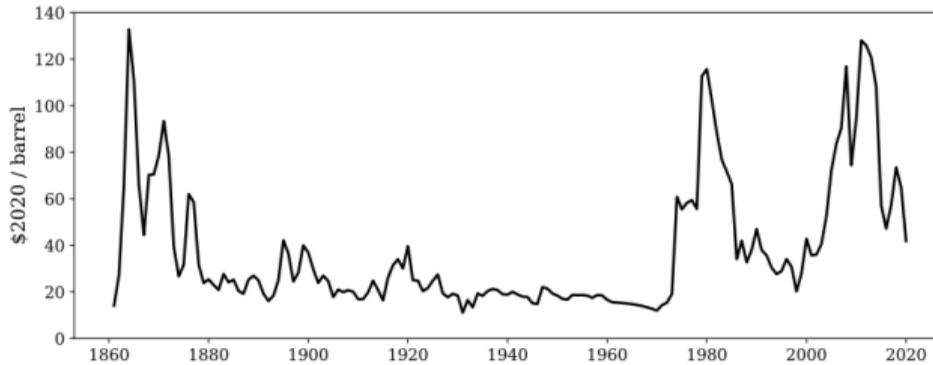


Figure 25.8: Crude oil price.

Source: BP (2021).

Figure: (BP, 2021)



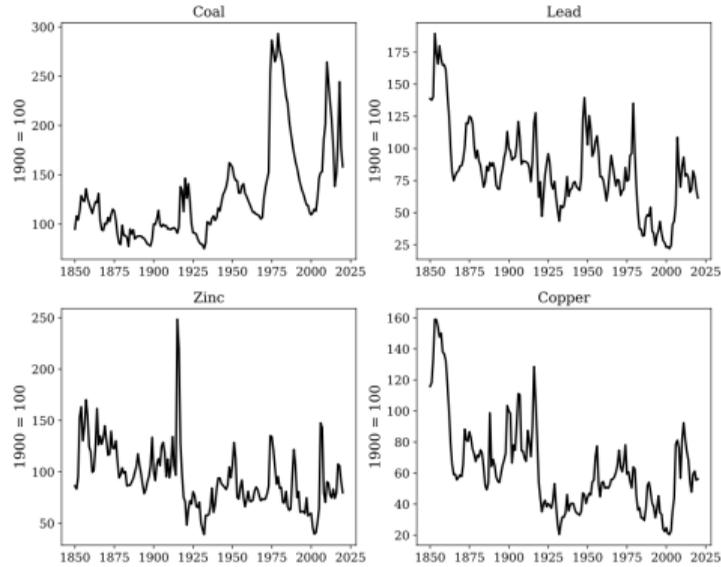


Figure 25.9: Inflation-adjusted prices for natural resources.

Source: Jacks (2019).

Figure: (Jacks, 2019)



Empirical Patterns

- **Energy use** (U.S., world):
 - Rapid increase in fossil fuel consumption historically.
 - Per capita oil use peaked in some regions (1970s).
- **Resource prices:** famously volatile (oil, metals, etc.), but no strong deterministic trend (some argue mild upward trend for oil post-WWII).
- **Challenge:** Basic Hotelling analysis would suggest a rising price path if the resource is scarce and extraction cost is constant, yet data show large volatility.



Hotelling's Rule

- **Cake-eating model** (no extraction cost):

$$\max \sum_{t=0}^{\infty} \beta^t \ln(c_t), \quad \text{s.t.} \quad \sum_{t=0}^{\infty} c_t = R_0.$$

Solution: $c_t = (1 - \beta)\beta^t R_0$.

- **Market equilibrium:** The resource price in present-value terms must be constant over time if there is no cost of extraction.

$$p_{t+1} = (1 + r) p_t, \quad \text{with } r = \frac{\beta}{1 - \beta} \text{ or so, depending on the setup.}$$

- **Extraction cost or partial equilibrium:** if cost mc_t changes with time, it modifies the Hotelling relation: $p_t - mc_t$ must grow at interest rate r .



Resource Use in a Growth Model

- **Dasgupta-Heal model:**

$$\max \sum_{t=0}^{\infty} \beta^t \ln(c_t), \quad c_t + k_{t+1} = A k_t^\alpha e_t^\nu, \quad \sum e_t = R_0.$$

- **Cobb-Douglas results:**

- $e_t = (1 - \beta)\beta^t R_0$: resource depletion path (similar to cake-eating).
 - If A grows over time, or if capital accumulates, net output grows even with finite resource.
 - Resource price grows at rate r .
- **Key policy insight:** with well-defined property rights, the competitive outcome can be *efficient* (no externality if no other side effects).



Short-Run vs. Long-Run Substitution

- **Empirical observation:** in the short run, capital and energy may be near complements (low elasticity). Over the long run, technologies adapt (higher elasticity).
- **Leontief example:**

$$Y_t = \min\{A k_t^\alpha, e_t\}.$$

- If resource is abundant early, e_t can grow with capital.
 - Eventually resource constraints bind $\rightarrow e_t$ must fall.
- **CES approach:**

$$Y_t = \left[\theta (K_t^\alpha L_t^{1-\alpha})^{\frac{\epsilon-1}{\epsilon}} + (1-\theta) (A_e e_t)^{\frac{\epsilon-1}{\epsilon}} \right]^{\frac{\epsilon}{\epsilon-1}}.$$

- $\epsilon > 1$ for strong complementarity, $\epsilon = 1$ for Cobb-Douglas, etc.



Endogenous, Directed Technical Change

- **Evidence:**
 - Historically, high fossil fuel prices triggered *energy-saving* innovations.
 - Post-1970s: energy use per capita declined in some countries, but *energy efficiency* soared.
- **Modeling approach:**
 - Romer/Aghion-Howitt style R&D framework with multiple sectors: capital-labor augmenting vs. energy-augmenting technologies.
 - R&D resources shift toward the most profitable type of innovation.
- **Implication:** Over the long run, the effective substitutability is higher due to *directed* R&D: more energy-saving innovations if fossil fuels are scarce/expensive.



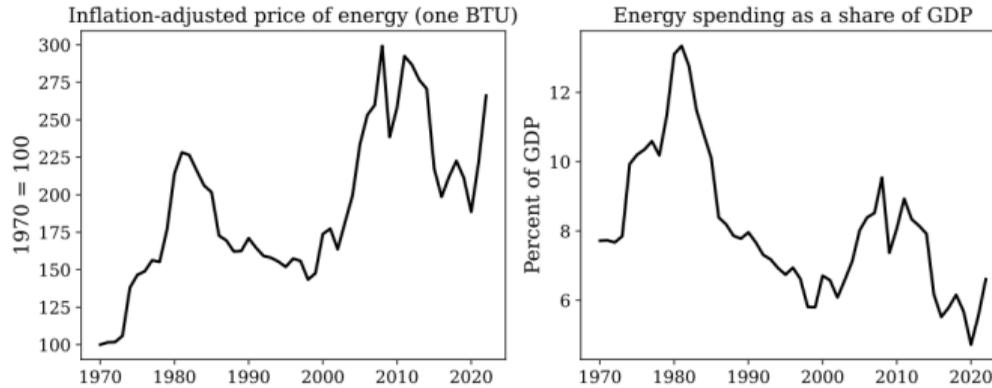


Figure 25.10: The price of fossil energy and its cost share.



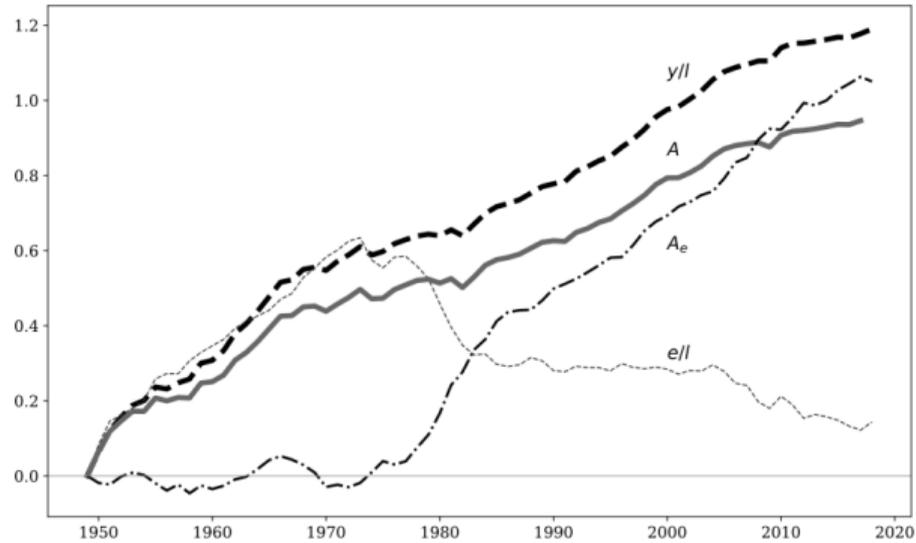


Figure 25.11: U.S. output, energy consumption and technological progress



Concluding Observations on Finite Resources

- **Market-based management:** With well-defined property rights, resource owners have incentive to optimize extraction over time (Hotelling logic).
- **No externality here means no direct policy needed** beyond typical market function.
- **Reality check:**
 - Costs of extraction vary, new discoveries occur, large price volatility is observed.
 - Directed technical change can ease scarcity constraints, enabling continued growth.
- **Bottom line:** Resource scarcity alone need not halt growth. But *environmental externalities* (like climate change) require policy.



Chapter Summary

- **Climate change and sustainability** are key macroeconomic issues.
- **IAMs** integrate a *growth model* with *carbon cycle & climate module* to study:
 - How emissions affect warming.
 - How warming impacts economic outcomes (damages).
 - Optimal policy design (e.g., carbon tax).
- **Key lessons:**
 1. A **Pigouvian carbon tax** can substantially reduce temperature rise with small short-run economic cost.
 2. Fossil fuels are large but finite: *Hotelling's rule* helps conceptualize resource depletion and price paths.
 3. **Energy-saving technical change** can mitigate scarcity and reduce damage from resource constraints.
- **Open questions:** discounting policy for future generations, uncertain climate feedbacks, catastrophic risks, distributional impacts, political economy of global agreements.



References I

- Administration, T. E. I. (2012). The annual energy review 2011. Online document.
- BGR (2020). Bgr energy study 2019 – data and developments concerning german and global energy supplies (23). Online document.
- BP (2021). Statistical review of world energy 2021, 70th edition. Online document.
- Golosov, M., Hassler, J., Krusell, P., and Tsyvinski, A. (2014). Optimal taxes on fossil fuel in general equilibrium. *Econometrica*, 82:41–88.
- Howard, P. H. and Sterner, T. (2017). Few and not so far between: A meta-analysis of climate damage estimates. *Environmental and Resource Economics*, 68:197–225.
- Jacks, D. (2019). From boom to bust: A typology of real commodity prices in the long run. *Cliometrica*, 13(2):202–220.
- Nordhaus, W. D. and Moffat, A. (2017). A survey of global impacts of climate change: Replication, survey methods, and a statistical analysis. *Working Paper 31323, National Bureau of Economic Research*.
- Rogner, H.-H. (1997). An assessment of world hydrocarbon resources. *Annual Review of Energy and the Environment*, 22(1):217–262.



Thank you!

Questions or comments?

orhan.torul@bogazici.edu.tr

